

ASTR 2500 - Solar System & Exoplanets

$$\bar{F} = \frac{L}{A} = \frac{L}{4\pi d^2} ; \text{ flux}$$

$$L_{\text{sun}} = A \sigma_{\text{sun}} T^4 = 4\pi R^2 \sigma_{\text{sun}} T^4 ; \text{ BB Luminos.}$$

Sun produces L_{\odot} energy / time

Maximum energy a planet can absorb / reflect
is $F(d) \cdot \text{cross-section} (\sigma_p)$

$$\frac{L_{\odot}}{4\pi d_p^2} \pi R_p^2 = \frac{1}{4} L_{\odot} \left(\frac{R_p}{d_p}\right)^2$$

Define albedo as fraction of light reflected:
 $A = \frac{E_{\text{reflected}}}{E_{\text{incident}}}$

Rate of energy absorption by planet is

$$\begin{aligned} W_p &= F(d) \cdot \sigma_p (1-A) \\ &= \frac{1}{4} L_{\odot} \left(\frac{R_p}{d}\right)^2 (1-A) \end{aligned}$$

If planet emits absorbed radiation like a BB, $W_p = L_p = 4\pi R_p^2 \sigma_{SB} T_p^4$
 $= \frac{1}{4} L_0 \left(\frac{R_p}{d}\right)^2 (1-A)$

$$T_p = \left(\frac{R_0}{d}\right)^{1/2} \left(\frac{1-A}{4}\right)^{1/4} T_0$$

Earth: $T_p \approx 250K = -23^\circ C = \underline{-9^\circ F}$

★ Why isn't Earth this cold???

★ Why don't astronauts on the Moon freeze on the surface?

To do calculation, need the distance

- use radar: send pulse + wait for it to reflect + return

- use Kepler's 3rd law

$$\left(\frac{P}{yr}\right)^2 = \left(\frac{a}{AU}\right)^3$$

Other fundamental properties: mass, dens.

(infer what they're made of)

$$p^2 = \frac{4\pi^2}{G(M+m)} a^3$$

planet \nearrow \nwarrow satellite $m \ll M$

$$M_p \approx \frac{4\pi^2 a^3}{G p^2}$$

What about radius? Use angular size

$R_p \approx \theta d$; d is distance from us, but can figure out

The density is then $\rho = \frac{M}{V}$

$$\rho = \frac{M_p}{\frac{4}{3}\pi R_p^3}$$

Rocky: $\rho = 3000 - 5500 \text{ kg m}^{-3}$

Gas: $\rho = 700 - 2000 \text{ kg m}^{-3}$

H_2O : $\rho = 1000 \text{ kg m}^{-3}$

Detecting Exoplanets

