ASTR 4080 - Week 12 Flatuess Problem Friedran Eq. can also le mitter $as \frac{H^{2}}{H_{0}^{2}} = Z S Z_{i}(a) + \frac{1 - \Omega_{0}}{a^{2}} (S.81)$ = Strage + Strage (observed ral) $1 - \Omega(t) = \frac{(1 - \Omega_{2})a^{2}}{\Omega_{r,0} + a\Omega_{r,0}}$ as al, (-SL(t) also & from its small value 1-520 arn~ 3×10-4 : 11-2-1 2×10-6 and ~ 3.6× (0-2: [[- Shoul] 2 7+(0) - extrapolate back to tp - 5×10-44, ap ~ 2×(0-32: [1-52, |<7.×(0-62 A Seens very improbable, BUT han do you calculate probabilities? (Kind of thing Hanking's last paper addressed) NEXT SLIDE

Harizan Problem CMB cames from the surface of last scatteri-s @ fls $\lambda_{hor}(t_{ks}) = \alpha(t_{ks}) c \int_{a}^{t_{ks}} \frac{dt}{\alpha(t)}$ a=0-> als is first rad, dominated a & th adthe matter-dan. i a & t^{2/3} De the integral & set Ahor (the) = 2.24 ctres = 0.251 mpc Har lig is that on the sky? Ask has to compute $\Theta_{har} = \frac{d_{har}(t_{AS})}{d_{A}} = \frac{0.251 \,\mu_{pc}}{12.8 \,\mu_{pc}} \approx \boxed{1.10}$ 41,253 deg? of slog, so ~ 40k acrusal regions Next Slide

Monopole P-oblem
Expect I per cansally-connected volume

$$V_{GUT} = 2 c t_{GUT}$$
, $t_{GUT} \sim 10^{-36} s$
 C_{ctool} $N_{nonopoles}(t_{GUT}) \sim \frac{1}{V} \sim 10^{\frac{92}{n}-3}$
 $c_{r}(t_{GUT}) \sim \frac{10^{104}}{10^{4}} \sim \frac{1}{T_{eV}} \frac{10^{92}}{m^{3}}$
 $E_{r}(t_{GUT}) \sim \frac{10^{104}}{10^{14}} \sim \frac{1}{T_{eV}} \frac{10^{97}}{m^{3}}$
Monopoles would have dominated evolution
 of universe after 10 s
 $Obs. : Space (5 \times 10^{-16})$

Properties of inflation &HERE Accel. Eq.: $\frac{a}{a} = -\frac{4\pi 6}{7^{-2}} \left(\xi + 3P \right)$ need a > 0, so $p < -\frac{2}{3}$ $p = w \mathcal{E}$, so $w - \frac{1}{3}$ La cosmol. const. Ni can do it (-=-1) If dominant, then $\frac{\ddot{a}}{a} = \frac{\Lambda_i}{3} (30)$ Friedran E_2 : $\left(\frac{\dot{n}}{a}\right)^2 = \frac{\Lambda_i}{2} = const. = H_i^2$ $\frac{d}{dt} = \int \frac{\Lambda_i}{\Lambda_i} dt = H_i dt$ $\left(a\left(f\right) \propto e^{H_{i}t}\right)$ At earliest files, rad. dan. b/c $\xi \ \alpha \ \alpha^{-4}$ So $a(f) = \begin{cases} a_i (t/\epsilon_i)^{1/2} & t \ 2t_i \\ a_i c & H_i(t_f - \epsilon_i) \\ a_i c & (t/\epsilon_f)^{1/2} & t \ 2t_f \end{cases}$ a(f)

Space increases in size during inflation

$$\frac{a(t_f)}{a(t_i)} = \frac{a_i e^{H_i(t_f - t_i)}}{a_i} = e^{H_i(t_f - t_i)}$$

$$= e^{N} \left(N = \# e - f_i d_{i_g s} \right)$$

Flatures Problem Meschad

$$\begin{aligned}
\left| 1 - \Omega \right| &= \frac{c^2}{R_o^2 a(t)^2 H(t)^2} \quad & \mathcal{L} e^{-2H_i t} \\
& \nabla e^$$

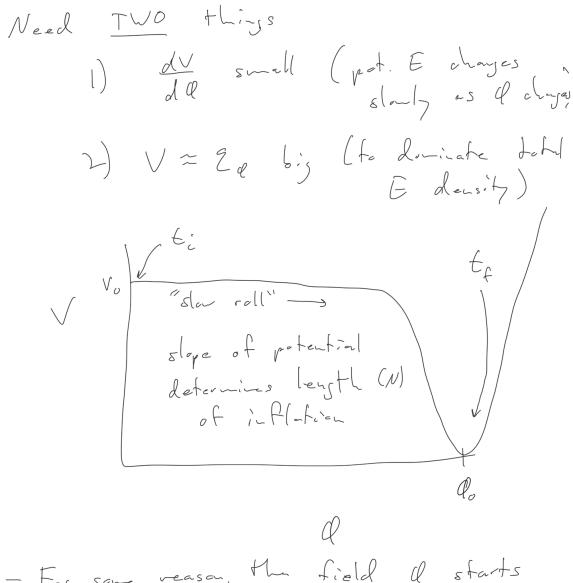
Since
$$|1-R_0| \ge 0.005$$
, can infor what N
 $N = 60$ ($c^{60} \sim 10^{26}$) $c^{2N} \approx 10^{52}$ $S = 0^{-28}$

Harizon Problem Resolved $d_{hor}(t) = a(t)c \int_{0}^{t} \frac{df}{a(t)}$ $= a_i c \left(\begin{array}{c} t_i & d_i t \\ a_i (t/t_i) \right)'^2 = 2c t_i^2$ dur (tE) = ai er c [2ti t (tf df time Hilt-ti)] Manopoles : Whited - 5×10-16 Myc-= e c [2f; + H;] t;= 10 s → 2ct; ~ 6×10 - 28 $H_{i}^{-1} - t_{i}$, $d_{\mu\nu}(f_{f}) = 2ct_{i}e^{\nu}$ t ctie () = //5m) N=60 Current harizon (196kc), af ~2×10-27 $d_{p}(t_{c}) = a_{f} d_{p}(t_{c}) \sim 0.9 \text{ m}$ $d_{r}(t_{c}) = e^{-N} d_{p}(t_{f}) \sim \frac{14 \times 10^{-29}}{14 \times 10^{-29}}$

Physics of Inflation
Universe has some indefinite period of
exp. expansion, then stypes somehan
Can imagine on "inflatan field" (a
new field/perturbe like the Higss)
Ly has a value
$$\mathcal{C}$$
 and point in space
 $\mathcal{Q}(\vec{r}, t)$
Elandin Ex: \mathcal{Q} must al
 $V(\mathcal{Q}) = 5 \mathcal{Q}$
 $V(\mathcal{Q}) = 5 \mathcal{Q}$
 $V(\mathcal{Q}) = 5 \mathcal{Q}$
 $V = E_{\mathcal{Q}} = \frac{1}{2tc^3} \hat{\mathcal{Q}}^2 + V(\mathcal{Q})$
 $\mathcal{Q} \Rightarrow E = tc^3 \hat{\mathcal{Q}}^2 - V(\mathcal{Q})$
 $\mathcal{Q} = \frac{1}{2tc^3} \hat{\mathcal{Q}}^2 - V(\mathcal{Q})$

If q alwayes slanly white q is small +;f;fs ccticV(e) $f_{m} = \mathcal{E}_{e} \approx \mathcal{V}(e) + \mathcal{P}_{e} \approx - \mathcal{V}(e)$ so beloves liler v=-1 Can use the fluid eq. : 2+3 a (2+P)=C $L/\dot{\epsilon}_{\varrho} = \frac{L}{\hbar c^{3}}\dot{\varrho}\dot{\varrho} + \frac{lv}{d\varrho}\dot{\varrho}$, so $\oint \left(\frac{\dot{\varphi}}{\pi c^3} + \frac{dv}{d\varphi}\right) + 3H(f)\left(\frac{\dot{\varphi}^{4}}{\pi c^3}\right) = 0$ \ddot{Q} + 3H \dot{Q} + $t_{c}^{3}\frac{dv}{dQ} = 0$ Size of Hubble paramter imposes a "frichiend" - speed is x = mg (1-e-kt/m) force Lo too, reach "terminal reforcity" - similarly, $\dot{Q} = -\frac{t_c^3}{3H}\frac{dV}{dR}\left(\pm\dot{Q}=0\right)$

We need
$$\frac{d^2}{dt^2} = \frac{d^2}{dt^2} \int_{t=0}^{t=2} \int_{t=0$$



- For some reason, the field of starts out out-of-equilibrium, in a TE state - "retastable false racum state"

Q = 0 Q start, it will roll down
tamed the min. in V (sim the local
clipe)
Lond dynamically important until its
E. density Ep = Vo dominates mediction
E. density Ep = Vo dominates mediction
E. ~ dT⁴, so Vo > dT⁴
which lypens Q
Ti = 2×10² °K (
$$\frac{V_0}{10^{105}}$$
 TV - 3)
ti ~ 3×10⁻³⁶ K ($\frac{V_0}{10^{105}}$ TV - 3)
M (leyth of 1.flatia) depends on shape
of V(Q), -/ T Vo, do sining TN
Embady, V=0 + Q = Qo, 1.4 not -lo modul
to oscillations (danged by 14 (friction true))
Locan happen faster if Q carpled to other
fields, like Vs (so E in V converted to
For the form after mixing at Ts)
R cluets universe after mixing at Ts)
R cluets universe after mixing at these

ASTR 4080 - Week 9