ASTR 4080 - Week 12

"Overdonsities" lead to collapse

Static + Longereons

 $n = -\frac{G(\Delta n)}{R^2}$

> extra mass over

 $p = \frac{M}{\frac{4}{3}\pi R^3}$

 $\frac{1}{p(1+f)} = \frac{M+\Delta M}{\frac{4}{3}\pi R^3} \Rightarrow p f = \frac{\Delta M}{\frac{4}{3}\pi R^3}$

 $\frac{1}{2}(t) = -\frac{4\pi G \overline{p}}{3} f(t)$

extra wass causes

R(t), f(t) > med mother egn.

What relates was I radius?

Veans Length > any pertubation will gran exponentially, faster in a donser environment BUT: Lill be affret by pressure non-vel: $w \approx \frac{|c|}{mc^2} \left(\sim 10^{-12} \text{ in this } \right)$ Pressure 1 as sphere collapses, able to support 1 gravity IF pressure gradieus has anough fine to establish itself La alle to commicate collapse is happening (tequilibrate) Edga > to

can define the size where this occurs: to -tdyn, to = 1/5 So $\lambda_{\overline{J}} \sim c_{\overline{S}} t_{dyn} \sim c_{\overline{S}} \left(\frac{1}{6\overline{\epsilon}}\right)^{1/2} \sim c_{\overline{S}} \left(\frac{c^{2}}{6\overline{\epsilon}}\right)^{1/2}$ that this collapse \\ \J = 27 Cs tayn (air: 15-10) But this is static case 7 our universe is expanding! texpand ~ H-1 = (302)/2 $t_{dyn} = \left(\frac{c^2}{4\pi G \Xi}\right)^{1/2} = \left(\frac{2}{3}\right)^{1/2} H^{-1}$ $\left(\right)_{J} = 2\pi \left(\frac{2}{3} \right)^{1/2} \sqrt{\sqrt{H}} \left(\frac{C}{H} \right)$ For baryons, can convert to the Tears mess

MJ=P1=7 (311 /J3)

Before decompling, baryons were dessed

along by rediction, so NJ + Mij

leternined by w = \frac{1}{3} > M_1 ~ 10 Me

After decompling, w = \frac{1cT}{mc^2} < C \frac{1}{3}

~ 10^{-5}

so M_1 ~ 10^5 Mo > flockations

large than present day star clusters

can collapse gravitationally

To follow the growth of perharbations I, need to include expansion since tirescale /H is confavable to the Neutarian analoss (splur again) $\vec{R} = -\frac{GM'}{R^2} = -\frac{G(M + GM)}{R^2} = -\frac{4\pi}{3}G_pR(1)$ $\frac{R}{R} = -\frac{4\pi}{3}6p - \frac{4\pi}{3}6p \delta$ Again, home mass conservation so $R(t) = R_0 \left[1 + \delta \right]^{-1/3} \propto \overline{p(t)}^{-1/3} \left[1 + \overline{f(t)} \right]$ $\bar{p} \propto q^{-3} \rightarrow \left[R(t) \propto a(t) \left[1 + f(t) \right]^{-1/3} \right]$ The derives again in $\hat{R} = \hat{a} \left(|f \right)^{-1/3} - \frac{1}{3} a \hat{s} \left(|f \right)^{-1/3}$ is = a (1+6) - 3 a f (1+6) -4/3 - \frac{1}{2} a f (1 $-\frac{1}{3}a(1+\delta)^{-4/3}|\hat{s}-\frac{4}{3}|\hat{s}'-\frac{4}{3}|\hat{s}'|$ $R = \frac{2}{3} + \frac{2}{3} +$ 1+5~1, 52<6 so set

$$\frac{R}{R} = \frac{a}{a} - \frac{1}{3}\dot{S} - \frac{2}{3}\frac{\dot{a}}{a}\dot{S} = -\frac{4\pi}{3}G_{p}$$

$$-\frac{4\pi}{3}G_{p} - \frac{4\pi}{3}G_{p} -$$

Radiahien epoch: SZ_CCI + n x E'12 so H= = = = = t -1 + find 1, + + 1 = 0 S(f) = B, +B2 lnt I sla grath of fluctuations by DM (which isn't compled to rad) Matter epoch: Sun 1 , H = 3+ $S + \frac{4}{3f}S - \frac{2}{2f^2}S = 0$ f(t) = 0, f2(3 + 02 f-1 inputant after some sout S x t 2/3 x a(t) x /1+2 (8<<1) DM stats @ Zrm = 3440, while baryons have to vait until Zlee ~ 1090

Slides